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Types of Search

Uninformed: use only information available in problem definition

Heuristic: exploits some knowledge of the domain

Uninformed search strategies

1. Breadth-first search

- 2. Uniform-cost search
- 3. Depth-first search
- 4. Depth-limited search
- 5. Iterative deepening depth-first search
- 6. Bidirectional search

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4

Search strategies

Criteria for evaluating search:

- 1. Completeness: does it always find a solution if one exists?
- 2. Time complexity: number of nodes generated/expanded
- 3. Space complexity: maximum number of nodes in memory
- 4. Optimality: does it always find a least-cost solution?

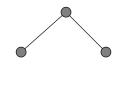
Time/space complexity measured in terms of:

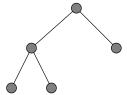
- ullet b: maximum branching factor of the search tree
- d: depth of the least-cost solution
- m: maximum depth of the search space (may be ∞)

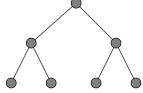
Breadth-first search (I)

- \rightarrow Expand root node
- \rightarrow Expand <u>all</u> children of root
- \rightarrow Expand each child of root
- \rightarrow Expand successors of each child of root, etc.

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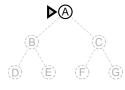
- \longrightarrow Expands nodes at depth d before nodes at depth d+1
- Systematically considers all paths length 1, then length 2, etc.
- → Implement: put successors at end of queue.. FIFO

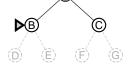
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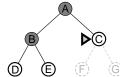
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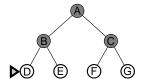
Breadth-first search (2)

6









Breadth-first search (3)

- \longrightarrow One solution?
- → Many solutions? Finds shallowest goal first
- 1. Complete? Yes, if b is finite
- 2. Optimal? provided cost increases monotonically with depth, not in general
- 3. Time? $1+b+b^2+b^3+\ldots+b^d+b(b^d-1)=O(b^{d+1})$ $O(b^{d+1}) \left\{ \begin{array}{l} \text{branching factor } b \\ \text{depth } d \end{array} \right.$
- 4. Space? same, $O(b^{d+1})$, keeps every node in memory, big problem can easily generate nodes at 10 MB/sec so 24 hrs = 860 GB

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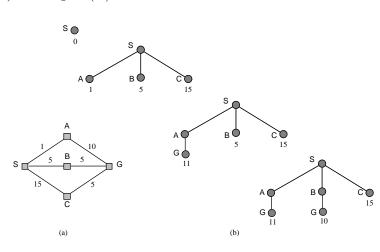
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Uniform-cost search (I)

- \longrightarrow Breadth-first does not consider path cost g(x)
- \longrightarrow Uniform-cost expands first lowest-cost node on the fringe
- → Implement: sort queue in decreasing cost order

When $g(x) = \text{Depth}(x) \longrightarrow \text{Breadth-first} \equiv \text{Uniform-cost}$

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Uniform-cost search (2)

- 1. Complete? Yes, if $cost \ge \epsilon$
- 2. Optimal?

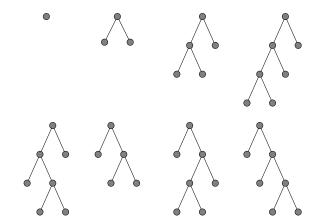
 If the cost is a monotonically increasing function

 When cost is added up along path, an operator's cost?
- 3. Time? $\# \text{ of nodes with } g \leq \text{ cost of optimal solution, } O(b^{\lceil C^*/\epsilon \rceil})$ where C^* is the cost of the optimal solution
- 4. Space? $\# \text{ of nodes with } g \leq \text{ cost of optimal solution, } O(b^{\lceil C^*/\epsilon \rceil})$

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Depth-first search (I)

- ----- Expands nodes at deepest level in tree
- \longrightarrow When dead-end, goes back to shallower levels
- \longrightarrow Implement: put successors at front of queue.. LIFO



 \longrightarrow Little memory: path and unexpanded nodes For b: branching factor, m: maximum depth, space?

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10

Depth-first search (3)

Time complexity:

We may need to expand all paths, $O(b^m)$

When there are many solutions, DFS may be quicker than BFS When m is big, much larger than d, ∞ (deep, loops), .. troubles

 \longrightarrow Major drawback of DFS: going deep where there is no solution..

12

Properties:

- 1. Complete? No in infinite-spaces, complete in finite spaces
- 2. Optimal?
- 3. Time? $O(b^m)$ Woow.. terrible if m is much larger than d, but if solutions are dense, may be much faster than breadth-first
- 4. Space? O(bm), linear!

Woow..

Depth-limited search (I)

- → DFS is going too deep, put a threshold on depth!

 For instance, 20 cities on map for Romania, any node deeper than 19 is cycling. Don't expand deeper!
- \longrightarrow Implement: nodes at depth l have no successor

13

Properties:

- 1. Complete?
- 2. Optimal?
- 3. Time? (given l depth limit)
- 4. Space? (given l depth limit)

Problem: how to choose l?

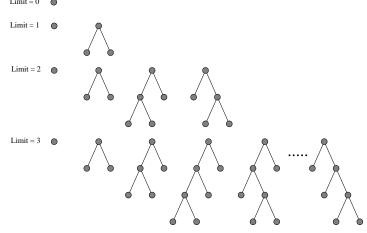
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Iterative-deepening search (I)

- \rightarrow DLS with depth = 0
- \rightarrow DLS with depth = 1
- \rightarrow DLS with depth = 2
- \rightarrow DLS with depth = 3...

14

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 $\stackrel{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\circ}}}} \stackrel{\circ}{\bigvee} \stackrel{\circ}{\longrightarrow} \text{Combines benefits of DFS and BFS}$

Iterative-deepening search (3)

— combines benefits of DFS and BFS

Properties:

- 1. Time? $(d+1).b^0 + (d).b + (d-1).b^2 + ... + 1.b^d = O(b^d)$
- 2. Space? O(bd), like DFS
- 3. Complete? like BFS
- 4. Optimal? like BFS (if step cost = 1)

Iterative-deepening search (4)

 \longrightarrow Some nodes are expanded several times, wasteful?

$$N(BFS) = b + b^2 + b^3 + ... + b^d + (b^{d+1} - d)$$

$$N(IDS) = (d)b + (d-1)b^2 + ... + (1)b^d$$

17

Numerical comparison for b = 10 and d = 5:

$$N(IDS) = 50 + 400 + 3,000 + 20,000 + 100,000 = 123,450$$

$$N(BFS) = 10 \, + \, 100 \, + \, 1,\!000 \, + \, 10,\!000 \, + \, 100,\!000 \, + \, 999,\!990 \, =$$

1,111,100

— IDS is preferred when search space is large and depth unknown

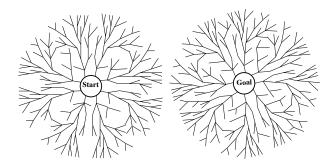
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Bidirectional search (I)

 \rightarrow Given initial state and the goal state, start search from both ends and meet in the middle

18



Instructor's notes #6 February 6, 2006 \rightarrow Assume same b branching factor, \exists solution at depth d, time: $O(2b^{d/2}) = O(b^{d/2})$

b = 10, d = 6, DFS = 1,111,111 nodes, BDS = 2,222 nodes!

Bidirectional search (2)

In practice :—(

- Need to define predecessor operators to search backwards If operator are invertible, no problem
- What if ∃ many goals (set state)? do as for multiple-state search
- need to check the 2 fringes to see how they match need to check whether any node in one space appears in the other space (use hashing) need to keep all nodes in a half in memory $O(b^{d/2})$
- What kind of search in each half space?

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Summary

Criterion	Breadth-	Uniform-	Depth-	Depth-	Iterative
	First	Cost	First	Limited	Deepening
Complete?	Yes*	Yes^*	No	Yes, if $l \ge d$	Yes
Time	b^{d+1}	$b^{\lceil C^*/\epsilon \rceil}$	b^m	b^l	b^d
Space	b^{d+1}	$b^{\lceil C^*/\epsilon ceil}$	bm	bl	bd
Optimal?	Yes*	Yes^*	No	No	Yes

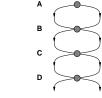
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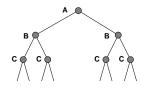
Instructor's notes #6 February 6, 2006 b branching factor d solution depth m maximum depth of tree l depth limit

Loops: (2)

Keep nodes in two lists: $\left\{ \begin{array}{l} \text{Open list: Fringe} \\ \text{Closed list: Leaf and expansed nodes} \end{array} \right.$

Discard a current node that matches a node in the closed list Tree-Search \longrightarrow Graph-Search





22

Issues:

- 1. Implementation: hash table, access is constant time Trade-off cost of storing+checking vs. cost of searching
- 2. Losing optimality when new path is cheaper/shorter of the one stored
- 3. BFS and IDS now require exponential storage

23

Summary

Path: sequence of actions leading from one state to another

Partial solution: a path from an initial state to another state

Search: develop a sets of partial solutions

- Search tree & its components (node, root, leaves, fringe)
- Data structure for a search node
- Search space vs. state space
- Node expansion, queue order
- Search types: uninformed vs. heuristic
- 6 uninformed search strategies
- 4 criteria for evaluating & comparing search strategies

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24

Searching with partial information (I)

So far, we assumed:

- Environment fully observable
- Environment deterministic
- Agent knows effects of actions

Thus, agent

- always knows where it is
- $\bullet\,$ can compute state where it will be after a sequence of actions

What happens when knowledge about states and actions is incomplete?

B.Y. Choueiry Searching with partial information (2) Incompleteness yields 3 types of problems: 25 • Sensorless (conformant) problems • Contingency problems • Exploration problems Instructor's notes #6 February 6, 2006 B.Y. Choueiry $Sensorless\ problems\ ({\rm conformant})$ • Environment not observable, no percepts 26 • Agent does not know in which exact state it is

- agent may be in one of more possible initial states

Instructor's notes #6 February 6, 2006 - an action may lead to one or more possible successor states

Contingency problems

27

- environment partially observable or actions are uncertain
- agent's percepts provide new input after each action, a contingency to plan for
- Adverserial problems: uncertainty caused by action of other agents

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Exploration problems

28

- States and actions of the environment are unknown
- Agent must act to discover them
- Extreme case of contingency problem

Sensorless problems (I)

Vacuum cleaner: no sensors, but agent knows effects of actions

29

Agent may be in any state {1, 2, 3, 4, 5, 6, 7, 8}

- [Right] always ends in $\{2, 4, 6, 8\}$
- [Right, Suck] always ends in $\{4, 8\}$
- [Right, Suck, Left, Suck] always works, coerces the world into 7

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Sensorless problems (2)

Environment not (fully) observable:

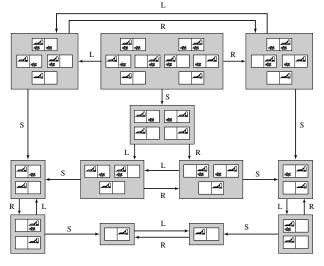
- Agent must think about sets of states,
- Agent has a belief state (set of possible states)

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Environment fully observable: 1 belief state has 1 state Solving sensorless problems: search in space of beliefs

- initial state is a belief state (all possible states)
- ullet actions map 1 belief state into another
- belief state is union of applying action to each state in initial belief state
- goal is reached when all states in belief state are goal states

vacuum cleaner: 12 belief states



In general:

 $8~\rm states,~2^8$ possible belief states

S states, 2^S possible belief states

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Sensorless problems (3)

So far assumed deterministic environment Approach/results hold for nondeterministic environment

32

Example: Murphy's law, Suck sometimes deposits dirt on carpet but only if there is no dirt there already

- [Suck] applied to State 4 leads to $\{2, 4\}$
- [Suck] applied to $\{1, 2, 3, 4, 5, 6, 7, 8\}$ leads to ...
- Problem is unsolvable (Exercise 3.18)!!

 Agent cannot tell whether state is dirty and cannot predict whether *Suck* is going to make it dirty or clean

 $\frac{3}{2}$

Contingency problems (I)

Environment partially observable or actions are uncertain

When agent can get some information:

- about environment
- from sensors
- after acting

Solution to a contingency problem is not a path, but a tree \longrightarrow branches are selected depending on percepts

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Contingency problems (2)

Example: vacuum cleaner

- has 'local dirt' sensor, no 'remote dirt' sensor
- has location sensor
- Murphy's law

34

- Now,
 - Agent perceives [L, Dirty], thinks in state $\{1, 3\}$
 - Action [Suck] leads to $\{5, 7\}$
 - Action [Suck, Right] leads to $\{6, 8\}$
 - Action [Suck, Right, Suck] leads to {8, 6} Plan can succeed (8), or fail (6)

Thus, action $[Suck, Right, \mathbf{if}[R, Dirty]\mathbf{then}Suck]$ leads to $\{8, 6\}$ Solution is a tree

Contingency problems (3)

Example: vacuum cleaner

- has 'local dirt' sensor and 'remote dirt' sensor
- has location sensor (fully observable)
- Murphy's law

Solution is a sequence of actions

Agent can proceed...

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Contingency problems (4)

In general, agent

- acts before having a guaranteed plan (solution is a tree)
- needs to consider every possibility that might arise
 - \longrightarrow may be an overkill

It is (sometimes) necessary to start acting, and deal with contingencies as they arise

- — Interleave Search and Execution
- — Useful for game playing and exploration problems

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